

# Three power-aware routing algorithms for sensor networks

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## Summary

This paper discusses online power-aware routing in large wireless ad hoc networks (especially sensor networks) for applications in which the message sequence is not known. We seek to optimize the lifetime of the network. We show that online power-aware routing does not have a constant competitive ratio to the off-line optimal algorithm. We develop an approximation algorithm called *max-min  $zP_{min}$*  that has a good empirical competitive ratio. To ensure scalability, we introduce a second online algorithm for power-aware routing. This hierarchical algorithm is called zone-based routing. Our experiments show that its performance is quite good. Finally, we describe a distributed version of this algorithm that does not depend on any centralization. Copyright © 2003 John Wiley & Sons, Ltd.

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## KEY WORDS

ad hoc network  
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## 1. Introduction

The proliferation of low-power analog and digital electronics has created huge opportunities in the field of wireless computing. It is now possible to deploy hundreds of devices of low computation, communication and battery power. They can create ad hoc networks and be used as distributed sensors to monitor large geographical areas, as communication enablers for field operations, or as grids of computation. These applications require great care in the utilization of power. The power level is provided by batteries and thus it is finite. Every message sent and every computation performed drains the battery.

In this paper we examine a class of algorithms for routing messages in wireless networks subject to power constraints and optimization. We envision a large ad hoc network consisting of thousands of computers as a sensor network distributed over a large geographical area. Clearly, this type of network has a high degree of redundancy. We would like to develop a power-aware approach to routing messages in such a system that is fast, scalable, and is online in that it *does not know ahead of time the sequence of messages* that has to be routed over the network.

The power consumption of each node in an ad hoc wireless system can be divided according to functionality into: (i) the power utilized for the transmission of a message; (ii) the power utilized for the reception of a message; and (iii) the power utilized while the system is idle. Table I lists power consumption numbers for several wireless cards. This suggests two complementary levels at which power consumption can be optimized: (i) minimizing power consumption during the idle time and (ii) minimizing power consumption during communication. In this paper we focus only on issues related to minimizing power consumption during communication—that is, while the system is transmitting and receiving messages. We believe that efficient message-routing algorithms, coupled with good solutions for optimizing power

consumption during the idle time will lead to effective power management in wireless ad hoc networks, especially for a sparsely deployed network.

Several metrics can be used to optimize power routing for a sequence of messages. Minimizing the energy consumed for each message is an obvious solution that optimizes locally the power consumption. Other useful metrics include minimizing the variance in each computer power level, minimizing the ratio of cost/packet, and minimizing the maximum node cost. A drawback of these metrics is that they focus on individual nodes in the system instead of the system as a whole. Therefore, routing messages according to these metrics might quickly lead to a system in which nodes have high residual power but the system is not connected because some critical nodes have been depleted of power. We choose to focus on a global metric by maximizing the lifetime of the network. We model this as the time to the earliest time a message cannot be sent. This metric is very useful for ad hoc networks in which each message is important and the networks are sparsely deployed.

In this paper we build on our previous work [4] and show that the online power-aware message routing problem is very hard (Section 3). This problem does not have a constant competitive ratio to the off-line optimal algorithm that knows the message sequence. Guided by this theoretical result, we propose an online approximation algorithm for power-aware message routing that optimizes the lifetime of the network and examines its bounds (Section 4). Our algorithm, called the *max-min  $zP_{min}$*  algorithm, combines the benefits of selecting the path with the minimum power consumption and the path that maximizes the minimal residual power in the nodes of the network. Despite the discouraging theoretical result concerning the competitive ratio for online routing, we show that the *max-min  $zP_{min}$*  algorithm has a good competitive ratio in practice, approaching the performance of the optimal off-line routing algorithm under realistic conditions.

Table I. Power consumption comparison among different wireless LAN cards [1–3]. For RangeLAN2, the power consumption for doze mode (which is claimed to be network aware) is 5 mA. The last one is Smart Spread Spectrum of Adcon Telemetry.

Card	Tr mA	Rv mA	Idle mA	Slp mA	Power Sup. V
RangeLAN2-7410	265	130	n/a	2	5
WaveLAN(11Mbps)	284	190	156	10	4.74
Smart Spread	150	80	n/a	5	5

Our proposed *max-min*  $zP_{min}$  algorithm requires information about the power level of each computer in the network. Having accurate knowledge of this information is not a problem in small networks. However, for large networks it is difficult to aggregate and maintain this information. This makes it hard to implement the *max-min*  $zP_{min}$  algorithm for large networks. Instead, we propose another online algorithm called *zone-based routing* that relies on *max-min*  $zP_{min}$  and is scalable (Section 5). Our experiments show that the performance of zone-based routing is very close to the performance of *max-min*  $zP_{min}$  with respect to optimizing the lifetime of the network.

Zone-based routing is a hierarchical approach in which the area covered by the (sensor) network is divided into a small number of zones. Each zone has many nodes and thus there is a lot of redundancy in routing a message through it. To send a message across the entire area we find a 'global' path from zone to zone and give each zone control over how to route the message within itself. Thus, zone-based power-aware routing consists of (i) an algorithm for estimating the power level of each zone; (ii) an algorithm for computing a path for each message across zones; and (iii) an algorithm for computing the best path for the message within each zone (with respect to the power lifetime of the zone.)

The algorithm *max-min*  $zP_{min}$  has the great advantage of not relying on the message sequence but the disadvantage of being centralized and requiring knowledge of the power level of each node in the system. These are unrealistic assumptions for field applications, for example, involving sensor networks in which the computation is distributed and information localized. The third type of routing we describe is a distributed version of our centralized algorithms. A distributed version of the *max-min*  $zP_{min}$  algorithm has the flavor of the distributed Bellman–Ford algorithm. This distributed algorithm requires  $n$  message broadcasts for each node if there is no clock synchronization, and only one message broadcast if the host clocks are synchronized.

## 2. Related Work

We are inspired by recent exciting results in ad hoc networks and in sensor networks. Most previous research on ad hoc network routing [5–13] focused on the protocol design and performance evaluation in terms of the message overhead and loss

rate. To improve the scalability of routing algorithms for large networks, many hierarchical routing methods have been proposed in [14–20]. In [21,22], zones, which are the route maintenance units, are used to find the routes. This previous work focused on how to find the correct route efficiently, but did not consider optimizing power while sending messages.

Singh *et al.* [23] proposed power-aware routing and discussed different metrics in power-aware routing. Some of the ideas in this paper are extensions of what that paper proposed. Minimal energy consumption was used in [24]. Stojmenovic and Lin proposed the first localized power-aware algorithm in their paper series [25]. Their algorithm is novel in combining the power and cost into one metric and running only on the basis of the local information. Chang and Tassiulas [26] also used the combined metric to direct the routing. Their algorithm is proposed to maximize the lifetime of a network when the message rate is known. Their main idea, that is, to avoid using low-power nodes and to choose the short path at the beginning, has inspired the approach described in this paper. We also use the same formula to describe the residual power fraction. The work presented in this paper is different from these previous results in that we develop online, hierarchical, and scalable algorithms that do not rely on knowing the message rate and optimize the lifetime of the network. In [27], Gupta and Kumar discussed the critical power at which a node needs to transmit in order to ensure the network is connected. Energy-efficient MAC layer protocols can be found in [28–30]. Wu *et al.* [31] proposed the power-aware approach in dominating set-based routing. Their idea is to use rules based on energy level to prolong the lifetime of a node in the refining process of reducing the number of nodes in the dominating set.

Another branch of the related work concerns optimizing power consumption during idle time rather than during the time of communicating messages [32,33]. These protocols put some nodes in the network into sleep mode to conserve energy, while maintaining the connectivity of the network to ensure communication. In a related work [31,34], Wu and Stojmenovic give an elegant solution by using connecting dominating sets, which generalize the idea of maintaining a connected network while keeping most of the nodes in sleeping mode. This work is complementary to the results of the idle-time power-conservation optimizing methods. Combined, efficient ways for

dealing with idle time and with communication can lead to powerful power-management solutions.

Work on reducing the communication overhead in broadcasting tasks [35] bears similarity with our approach to reducing the message broadcasting in routing application. In the paper by Stojmenovic *et al.*, a node will rebroadcast a message only if there are neighbors not covered by the previous broadcasts. In contrast, our distributed algorithms [36] eliminate the message broadcasts that are useless by discerning them with the message delay. As a result, in some of the algorithms we proposed, we can get a constant message broadcast for each node.

Related results in sensor networks include [37–42]. The high-level vision of wireless sensor networks was introduced in [37,38]. Achieving energy-efficient communication is an important issue in sensor network design. Using directed diffusion for sensor coordination is described in [39,40]. In [43] a low-energy adaptive protocol that uses data fusion is proposed for sensor networks. Our approach is different from the previous work in that we consider message routing in sensor networks, and our solution does not require to know or aggregate the data transmitted.

### 3. Formulation of Power-aware Routing

#### 3.1. The Model

Power consumption in ad hoc networks can be divided into two parts: (i) the idle mode and (ii) the transmit/receive mode. The nodes in the network are either in idle mode or in transmit/receive mode at all times. The idle mode corresponds to a baseline power consumption. Optimizing this mode is the focus of [31–34]. We instead focus on studying and optimizing the transmit/receive mode. When a message is routed through the system, all the nodes, with the exception of the source and destination nodes, receive a message and then immediately relay it. Because of this, we can view the power consumption at each node as an aggregate between transit and receive powers that we will model as one parameter.

More specifically, we assume an ad hoc network that can be represented by a weighted graph  $G(V, E)$ . The vertices of the graph correspond to computers in the network. They have weights that correspond to the computer's power level. The edges in the graph correspond to pairs of computers that are in communication range. Each edge weight is the power

cost of sending a unit message\* between the two nodes. Our results are independent of the power consumption model as long as we assume the power consumption of sending a unit message between two nodes does not change during a run of the algorithm. That is, the weight of any edge in the network graph is fixed.

Although our algorithms are independent of the power consumption model, we fixed one model for our implementation and simulation experiments. Suppose a host needs power  $e$  to transmit a message to another host who is  $d$  distance away. We use the model of [2,24,43] to compute the power consumption for sending this message:

$$e = kd^c + a$$

where  $k$  and  $c$  are constants for the specific wireless system (usually  $2 \leq c \leq 4$ ), and  $a$  is the electronics energy that depends on factors such as digital coding, modulation, filtering, and spreading of the signal. Since our algorithms can use any power consumption model, we use  $a = 0$  to simplify the implementation.

We focus on networks in which power is a finite resource. Only a finite number of messages can be transmitted between any two hosts. We wish to solve the problem of routing messages so as to maximize the battery lives of the hosts in the system. The lifetime of a network with respect to a sequence of messages is the earliest time when a message cannot be sent because of saturated nodes. We selected this metric under the assumption that all messages are important. Our results, however, can be relaxed to accommodate up to  $m$  message delivery failures, with  $m$  being a constant parameter.

#### 3.2. Relationship to Classical Network Flow

Power-aware routing is different from the maximal network flow problem although there are similarities. The classical network flow problem constrains the capacity of the edges instead of limiting the capacity of the nodes. If the capacity of a node does not depend on the distances to neighboring nodes, our problem can also be reduced to maximal network flow.

We use the following special case of our problem in which there is only one source node and one sink node to show that the problem is NP-hard. The

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\* Without loss of generality, we assume that all the messages are unit messages. Longer messages can be expressed as sequences of unit messages.

maximal number of messages sustained by a network from the source nodes to the sink nodes can be formulated as linear programming. Let  $n_{ij}$  be the total number of messages from node  $v_i$  to node  $v_j$ ,  $e_{ij}$  denote the power cost to send a message between node  $v_i$  to node  $v_j$ , and  $s$  and  $t$  denote the source and sink in the network. Let  $P_i$  denote the power of node  $i$ . We wish to maximize the number of messages in the system subject to the following constraints: (i) the total power used to send all messages from node  $v_i$  does not exceed  $P_i$  and (ii) the number of messages from  $v_i$  to all other nodes is the same as the number of messages from all other nodes to  $v_i$ , which are given below:

$$\begin{aligned} & \text{maximize } \sum_j n_{sj} \quad \text{subject to} \\ & \sum_j n_{ij} \cdot e_{ij} \leq P_i \end{aligned} \quad (1)$$

$$\sum_j n_{ij} = \sum_j n_{ji} \quad (\text{for } i \neq s, t) \quad (2)$$

This linear programming formulation can be solved in polynomial time. However, we need the integer solution, but computing the integer solution is NP-hard. Figure 1 shows the reduction to set partition for proving the NP-hardness of the integer solution.

### 3.3. Competitive Ratio for Online Power-aware Routing

In a system where the message rates are unknown, we wish to compute the best path to route a message.

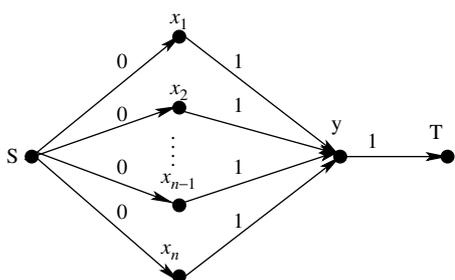


Fig. 1. The integer solution problem can be reduced to set partition as follows. Construct a network based on the given set. The power of  $x_i$  is  $a_i$  for all  $1 \leq i \leq n$ , and the power of  $y$  is  $\sum_{a_i \in A} a_i/2$ . The weight of each edge is marked on the network. For any set of integers  $S = a_1, a_2, \dots, a_n$ , we are asked to find the subset of  $S, A$  such that  $\sum_{a_i \in A} a_i = \sum_{a_i \in S-A} a_i$ . We can construct a network as depicted here. The maximal flow of the network is  $\sum_{a_i \in A} a_i/2$ , and it can only be gotten when the flow of  $x_i y$  is  $a_i$  for all  $a_i \in A$ , and for all other  $x_i y$ , the flow is 0.

Since the message sequence is unknown, there is no guarantee that we can find the optimal path. For example, the path with the least power consumption can quickly saturate some of the nodes. The difficulty of solving this problem without knowledge of the message sequence is summarized by the theoretical properties of its competitive ratio. The competitive ratio of an online algorithm is the ratio between the performance of that algorithm and the optimal off-line algorithm that has access to the entire execution sequence prior to making any decisions.

**Theorem 1** *No online algorithm for message routing has a constant competitive ratio in terms of the lifetime of the network or the number of messages sent.*

Theorem 1, whose proof is shown in Figure 2, shows that it is not possible to compute online an optimal solution for power-aware routing.

### 4. Online Power-Aware Routing with *max-min zP<sub>min</sub>*

In this section we develop an approximation algorithm for online power-aware routing and show experimentally that our algorithm has a good empirical competitive ratio and comes close to the optimal.

We believe that it is important to develop algorithms for message routing that do not assume prior knowledge of the message sequence because for ad hoc network applications this sequence is dynamic and depends on sensed values and goals communicated to the system as needed. Our goal is to increase the lifetime of the network when the message sequence is not known. We model lifetime as the earliest time that a message cannot be sent. Our assumption is that each message is important and thus the failure of delivering a message is a critical event. Our results can be extended to tolerate up to  $m$  message delivery failures, where  $m$  is a parameter. We focus the remaining of this discussion on the failure of the first message delivery.

Intuitively, message routes should avoid nodes whose power is low because overuse of these nodes will deplete their battery power. Thus, we would like to route messages along the path with the maximal minimal fraction of remaining power after the message is transmitted. We call this path the *max-min path*. The performance of max-min path can be very bad, as shown by the example in Figure 3. Another concern with the max-min path is that going

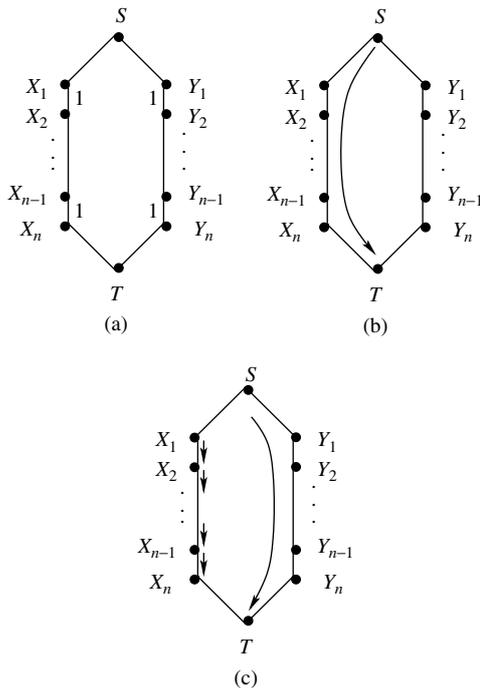


Fig. 2. In this network, the power of each node is  $1 + \epsilon$  and the weight on each edge is 1. (a) gives the network; (b) is the route for the online algorithm; and (c) is the route for the optimal algorithm. Consider the message sequence that begins with a message from  $S$  to  $T$ , say,  $ST$ . Without loss of generality (since there are only two possible paths from  $S$  to  $T$ ), the online algorithm routes the message via the route  $SX_1X_2X_3 \dots X_{n-1}X_nT$ . The message sequence is  $X_1X_2, X_2X_3, X_3X_4, \dots, X_{n-1}X_n$ . It is easy to see that the optimal algorithm [see (c)] routes the first message through  $SY_1Y_2Y_3 \dots Y_{n-1}Y_nT$ , then routes the remaining messages through  $X_1X_2, X_2X_3, X_3X_4, \dots$ , and  $X_{n-1}X_n$ . Thus the optimal algorithm can transmit  $n$  messages. The online algorithm (b) can transmit at most 1 message for this message sequence because the nodes  $X_1, X_2, \dots, X_n$  are all saturated after routing the first message. The competitive ratio is small when  $n$  is large.

through the nodes with high residual power may be expensive as compared to the path with the minimal power consumption. Too much power consumption decreases the overall power level of the system and thus decreases the lifetime of the network. There is a trade-off between minimizing the total power consumption and maximizing the minimal residual power of the network. We propose to enhance a max-min path by limiting its total power consumption.

The two extreme solutions to power-aware routing for one message are (i) compute a path with minimal power consumption  $P_{min}$  and (ii) compute a path that maximizes the minimal residual power in the network. We look for an algorithm that optimizes both

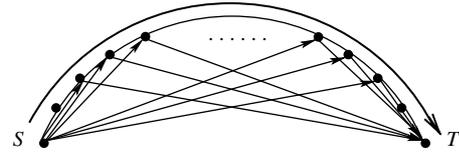


Fig. 3. The performance of the max-min path can be very bad. In this example, each node except for the source  $S$  has the power  $20 + \epsilon$ , and the weight of each edge on the arc is 1. The weight of each straight edge is 2. Let the power of the source be  $\infty$ . The network can send 20 messages from  $S$  to  $T$  according to the max-min strategy by taking the edges on the arc (see the arc on the top). But the optimal number of messages that follows the straight edges with black arrows is  $10(n - 4)$  where  $n$  is the number of nodes.

criteria. We relax the minimal power consumption for the message to be  $zP_{min}$  with parameter  $z \geq 1$  to restrict the power consumption for sending one message to  $zP_{min}$ . We propose an algorithm we call *max-min  $zP_{min}$*  that consumes at most  $zP_{min}$  while maximizing the minimal residual power fraction. The rest of the section describes the *max-min  $zP_{min}$*  algorithm, presents empirical justification for it, a method for adaptively choosing the parameter  $z$  and describes some of its theoretical properties.

The following notation is used in the description of the *max-min  $zP_{min}$*  algorithm. Given a network graph  $(V, E)$ , let  $P(v_i)$  be the initial power level of node  $v_i$ ,  $e_{ij}$  the weight of the edge  $v_i v_j$ , and  $P_t(v_i)$  is the power of the node  $v_i$  at time  $t$ . Let  $u_{ij} = (P_t(v_i) - e_{ij})/P(v_i)$  be the residual power fraction after sending a message from  $i$  to  $j$ .

**Algorithm 1** *max-min  $zP_{min}$ -path algorithm*

- 1: Find the path with the least power consumption,  $P_{min}$  by using the Dijkstra algorithm
- 2: **while** true **do**
- 3: Find the path with the least power consumption in the graph
- 4: **if** the power consumption  $> z \cdot P_{min}$  or no path is found **then**
- 5: the previous shortest path is the solution, stop
- 6: Find the minimal  $u_{ij}$  on that path, let it be  $u_{min}$
- 7: Find all the edges whose residual power fraction  $u_{ij} \leq u_{min}$ , remove them from the graph

Algorithm 1 describes the algorithm. In each round we remove at least one edge from the graph. The algorithm runs the Dijkstra algorithm to find the shortest path for at most  $|E|$  times where  $|E|$  is the number of edges. The running time of the Dijkstra

algorithm is  $O(|E| + |V| \log |V|)$  where  $|V|$  is the number of nodes. Then the running time of the algorithm is at most  $O(|E| \cdot (|E| + |V| \log |V|))$ . By using binary search, the running time can be reduced to  $O(\log |E| \cdot (|E| + |V| \log |V|))$ . To find the pure max–min path, we can modify the Bellman–Ford algorithm by changing the relaxation procedure. The running time is  $O(|V| \cdot |E|)$ .

#### 4.1. Adaptive Computation for $z$

An important factor in the *max–min*  $zP_{min}$  algorithm is the parameter  $z$  that measures the trade-off between the max–min path and the minimal power path. When  $z = 1$ , the algorithm computes the minimal power consumption path. When  $z = \infty$ , it computes the max–min path. We would like to investigate an adaptive way of computing  $z > 1$  such that *max–min*  $zP_{min}$  will lead to a longer lifetime for the network than each of the *max–min* and minimal power algorithms. Algorithm 2 describes the algorithm for adaptively computing  $z$ .  $P$  is the initial power of a host.  $\Delta P_t$  is the residual power decrease at time  $t$  compared to time  $t - T$ . Basically,  $P/\Delta P_t$  gives an estimation for the lifetime of that node if the message sequence is regular with some cyclicity. The adaptive algorithm works well when the message distributions are similar as time elapses.

##### Algorithm 2 Adaptive *max–min* $zP_{min}$ algorithm

- 1: Choose initial value  $z$ , the step  $\delta$
- 2: Run the *max–min*  $zP_{min}$  algorithm for some interval  $T$
- 3: Compute  $P/\Delta P_t$  for every host, let the minimal one be  $t_1$
- 4: **while** true **do**
- 5:   Increase  $z$  by  $\delta$ , and run the algorithm again for time  $T$
- 6:   Compute the minimal  $P/\Delta P_t$  among all hosts, let it be  $t_2$
- 7:   **if** some host is saturated **then**
- 8:     **exit**
- 9:   **if**  $t_1 < t_2$  **then**
- 10:      $t_1 = t_2$
- 11:   **if**  $t_1 > t_2$  **then**
- 12:      $\delta = -\delta/2$ ,  $t_1 = t_2$

We conducted several simulation experiments to evaluate the adaptive computation of  $z$ . In a first experiment we generated the positions of hosts in a square field randomly using the following parameters.

The scope of the network is  $10 * 10$ , the number of hosts in the network is 20, the power consumption weights for transmitting a message are  $e_{ij} = 0.001 * d_{ij}^3$ , and the initial power of each host is 30. Messages are generated between all possible pairs of hosts and are distributed evenly. Figure 4(a) shows the number of messages transmitted until the first message delivery failure for different values of  $z$ . Using the adaptive method for selecting  $z$  with  $z_{init} = 10$ , the total number of messages sent increases to 12,207, which is almost the best performance by *max–min*  $zP_{min}$  algorithm.

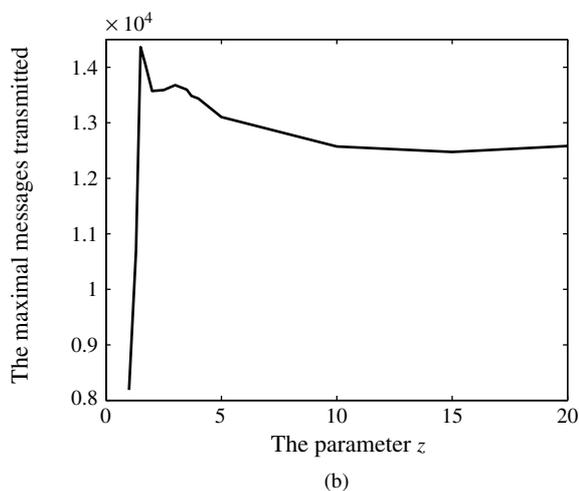
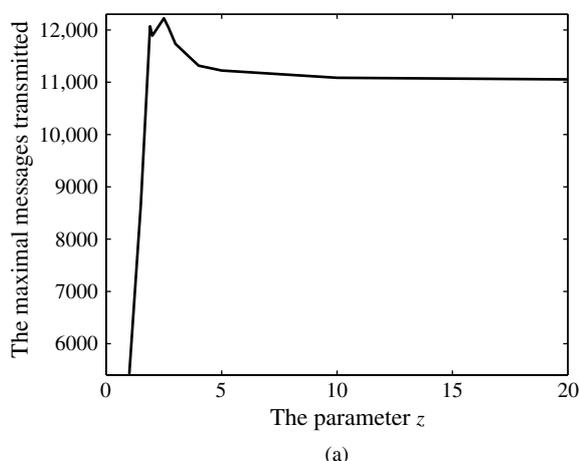


Fig. 4. The effect of  $z$  on the maximal number of messages in a square network space. The positions of hosts are generated randomly. In the first graph the network scope is  $10 * 10$ , the number of hosts is 20, the weights are generated by  $e_{ij} = 0.001 * d_{ij}^3$ , the initial power of each host is 30, and messages are generated between all possible pairs of the hosts and are distributed evenly. In the second graph the number of hosts is 40, the initial power of each node is 10, and all other parameters are the same as in the first graph.

In the second experiment, we generated the positions of hosts evenly distributed on the perimeter of a circle. The radius of the circle is 20, number of hosts 20; the weight formula:  $e_{ij} = 0.0001 * d_{ij}^3$ ; and the initial power of each host is 10. Messages are generated between all possible pairs of the hosts and are distributed evenly. The performance according to various  $z$  can be found in Figure 5(a). By using the adaptive method, the total number of messages sent until reaching a network partition is 11, 588, which is much better than in most cases when we choose a fixed  $z$ .

#### 4.2. Empirical Evaluation of the $max-min zP_{min}$ Algorithm

We conducted several experiments for evaluating the performance of the  $max-min zP_{min}$  algorithm.

In the first set of experiments (Figure 4), we compare how  $z$  affects the performance of the lifetime of the network. In the first experiment, a set of hosts are randomly generated on a square. For each pair of nodes, one message is sent in both directions for a unit of time. Thus, there is a total of  $n * (n - 1)$

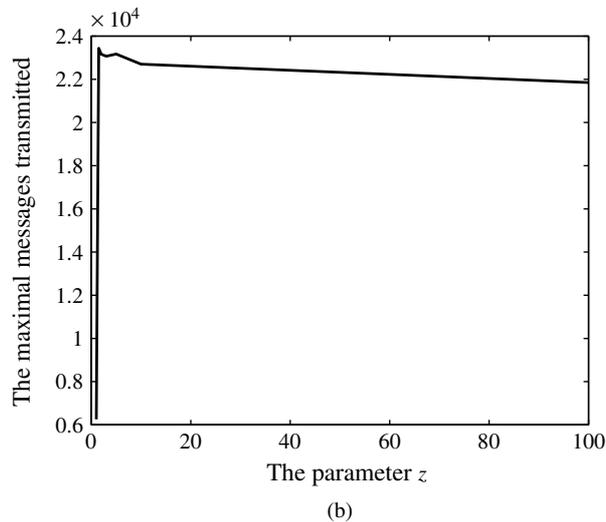
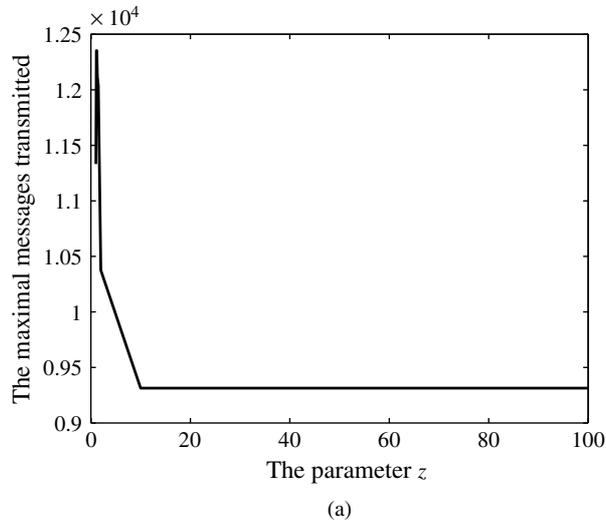


Fig. 5. (a) shows the effect of  $z$  on the maximal number of messages in a ring network. The radius of the circle is 20, the number of hosts is 20, the weights are generated by  $e_{ij} = 0.0001 * d_{ij}^3$ , the initial power of each host is 10 and messages are generated between all possible pairs of the hosts and are distributed evenly. (b) shows a network with four columns of the size  $1 * 0.1$ . Each area has 10 hosts that are randomly distributed. The distance between two adjacent columns is 1. (b) gives the performance when  $z$  changes. The vertical axis shows the maximal messages sent before the first host is saturated. The number of hosts is 40; the weight formula is  $e_{ij} = 0.001 * d_{ij}^3$ ; the initial power of each host is 1; messages are generated between all possible pairs of the hosts and are distributed evenly.

messages sent in each unit time, where  $n$  is the number of the hosts in the network. We experimented with other network topologies. Figure 5(a) shows the results obtained in a ring network. Figure 5(b) shows the results obtained when the network consists of four columns where nodes are approximately aligned in each column. The same method used in experiment 1 varies the value of  $z$ . These experiments show that adaptively selecting  $z$  leads to a superior performance over the minimal power algorithm ( $z = 1$ ) and the max-min algorithm ( $z = \infty$ ). Furthermore, when compared to an optimal routing algorithm, *max-min*  $zP_{min}$  has a constant empirical competitive ratio (see Figure 6a).

Figure 6(b) shows more data that compares the *max-min*  $zP_{min}$  algorithm to the optimal routing strategy. We computed the optimal strategy by using a linear programming package<sup>†</sup>. We ran 500 experiments. In each experiment a network with 20 nodes was generated randomly in a  $10 * 10$  network space. The messages were sent to one gateway node repeatedly. We computed the ratio of the lifetime of the *max-min*  $zP_{min}$  algorithm to the optimal lifetime. Figure 6 shows that *max-min*  $zP_{min}$  performs better than 80% of the optimal for 92% of the experiments and performs within more than 90% of the optimal for 53% of the experiments. Since the optimal algorithm has the advantage of knowing the message sequence, we believe that *max-min*  $zP_{min}$  is practical for applications in which there is no knowledge of the message sequence.

#### 4.3. Analysis of the *max-min* $zP_{min}$ Algorithm

In this section we quantify the experimental results from the previous section in an attempt to formulate more precisely our original intuition about the trade-off between the minimal power routing and max-min power routing. We provide a lower bound for the lifetime of the *max-min*  $zP_{min}$  algorithm as compared to the optimal solution. We discuss this bound for a general case in which there is some cyclicity to the messages that flow in the system and then show the specialization to the no-cyclicity case.

Suppose the message distribution is regular, that is, in any period of time  $[t_1, t_1 + \delta)$ , the message distributions on the nodes in the network are the same. Since in sensor networks we expect some sort of

<sup>†</sup> To compute the optimal lifetime, the message rates are known. The max-min algorithm does not have this information.

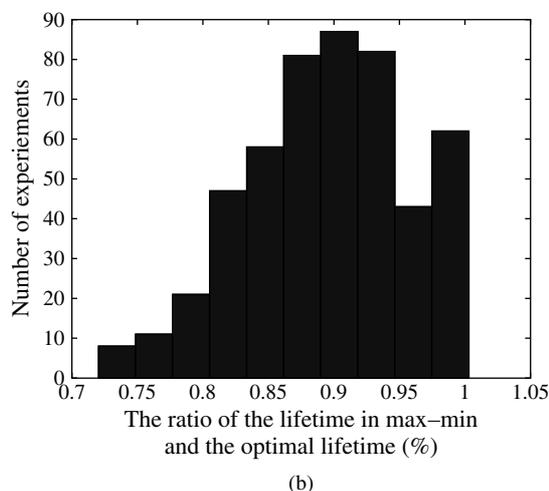
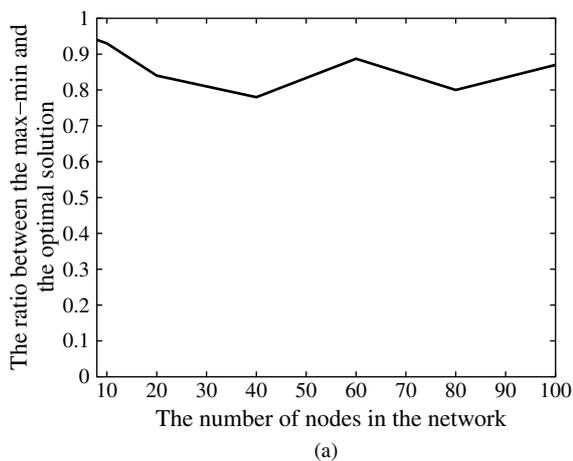


Fig. 6. (a) compares the performance of the *max-min*  $zP_{min}$  to the optimal solution. The positions of hosts in the network are generated randomly. The network scope is  $10 * 10$ , the weight formula is  $e_{ij} = 0.0001 * d_{ij}^3$ , the initial power of each host is 10, messages are generated from each host to a specific gateway host, the ratio  $z$  is 100.0. (b) shows the histogram that compares *max-min*  $zP_{min}$  to the optimal for 500 experiments. In each experiment the network consists of 20 nodes randomly placed in a  $10 * 10$  network space. The cost of messages is given by  $e_{ij} = 0.001 * d_{ij}^3$ . The hosts have the same initial power and messages are generated for hosts to one gateway host. The horizontal axis is the ratio between the lifetime of the *max-min*  $zP_{min}$  max-min algorithm and the optimal lifetime, which is computed off-line.

cyclicity for message transmission, we assume that we can schedule the message transmission with the same policy in each time slice we call  $\delta$ . In other words, we partition the time line into many time slots  $[0, \delta)$ ,  $[\delta, 2\delta)$ ,  $[2\delta, 3\delta)$ ,  $\dots$ . Note that  $\delta$  is the lifetime of the network if there is no cyclical behavior in message transmission. We assume the same messages are

generated in each  $\delta$  slot but their sequence may be different.

Let the optimal algorithm be denoted by  $O$ , and the *max-min*  $zP_{min}$  algorithm be denoted by  $M$ . In  $M$ , each message is transmitted along a path whose overall power consumption is less than  $z$  times the minimal power consumption for that message. The initial time is 0. The lifetime of the network by algorithm  $O$  is  $T_O$ , and the lifetime by algorithm  $M$  is  $T_M$ . The initial power of each node is:  $P_{10}, P_{20}, P_{30}, \dots, P_{(n-1)0}, P_{n0}$ . The remaining power of each node at  $T_O$  by running algorithm  $O$  is:  $P_{1O}, P_{2O}, P_{3O}, \dots, P_{n-1O}, P_{nO}$ . The remaining power of each node at  $T_M$  by running algorithm  $M$  is:  $P_{1M}, P_{2M}, P_{3M}, \dots, P_{n-1M}, P_{nM}$ . Let the message sequence in any slot be  $m_1, m_2, \dots, m_s$ , and the minimal power consumption to transmit these messages be  $P_{0m_1}, P_{0m_2}, P_{0m_3}, \dots, P_{0m_s}$ .

**Theorem 2**

The lifetime of algorithm  $M$  satisfies

$$T_M \geq \frac{T_O}{z} + \frac{\delta \cdot \left( \sum_{k=1}^n P_{kO} - \sum_{k=1}^n P_{kM} \right)}{z \cdot \sum_{k=1}^s P_{0m_k}} \quad (3)$$

**Proof:**

We have

$$\sum_{k=1}^n P_{k0} = \sum_{k=1}^n P_{kM} + \sum_{k=1}^{M_{T_M}} P_{Mm_k} = P_M$$

where  $M_{T_M}$  is the number of messages transmitted from time point 0 to  $T_M$ .  $P_{Mm_k}$  is the power consumption of the  $k$ th message by running algorithm  $M$ . We also have:

$$\sum_{k=1}^n P_{k0} = \sum_{k=1}^n P_{kO} + \sum_{k=1}^{M_{T_O}} P_{Om_k} = P_O$$

where  $M_{T_O}$  is the number of messages transmitted from time point 0 to  $T_O$ .  $P_{Om_k}$  is the power consumption of the  $k$ th message by running algorithm  $O$ .

Since the messages are the same for any two slots without considering their sequence, we can schedule the messages such that the message rates along the same route are the same in the two slots (think about dividing every message into many tiny packets, and average the message rate along a route in algorithm  $O$  into the two consecutive slots evenly). We have

$$\sum_{k=1}^{M_{T_O}} P_{Om_k} = \frac{M_{T_O}}{s} \cdot \sum_{k=1}^s P_{Om_k} = \frac{T_O}{\delta} \cdot \sum_{k=1}^s P_{Om_k}$$

and

$$\sum_{k=1}^{M_{T_M}} P_{Mm_k} = \sum_{j=1}^{T_M/\delta} \sum_{k=1}^s P_{Mmkj}$$

So we have:

$$P_O = \sum_{k=1}^n P_{kO} + \frac{T_O}{\delta} \cdot \sum_{k=1}^s P_{Om_k},$$

$$P_M = \sum_{k=1}^n P_{kM} + \sum_{j=1}^{T_M/\delta} \sum_{k=1}^s P_{Mmkj}$$

and

$$P_O = P_M$$

$P_{Mmkj}$  is the power consumption of the  $k$ th message in slot  $j$  by running algorithm  $M$ . We also have the following assumption and the minimal power of  $P_{0mk}$ . For any  $1 \leq j \leq \frac{T_M}{\delta}$  and  $k$ , we have only one corresponding  $l$ ,

$$P_{Mmkj} \leq z \cdot P_{0m_l} \text{ and } P_{0m_k} \geq P_{0m_l}$$

Then,

$$P_O \geq \sum_{k=1}^n P_{kO} + \frac{T_O}{\delta} \cdot \sum_{k=1}^s P_{0m_k}$$

$$P_M \leq \sum_{k=1}^n P_{kM} + \frac{z \cdot T_M}{\delta} \cdot \sum_{k=1}^s P_{0m_k}$$

Thus,

$$\sum_{k=1}^n P_{kM} + \frac{z \cdot T_M}{\delta} \cdot \sum_{k=1}^s P_{0m_k} \geq \sum_{k=1}^n P_{kO} + \frac{T_O}{\delta} \cdot \sum_{k=1}^s P_{0m_k}$$

We have:

$$T_M \geq \frac{T_O}{z} + \frac{\delta \cdot \left( \sum_{k=1}^n P_{kO} - \sum_{k=1}^n P_{kM} \right)}{z \cdot \sum_{k=1}^s P_{0m_k}}$$

□

Theorem 2 gives us insight into how well the message-routing algorithm does with respect to optimizing the lifetime of the network. Given a network topology and a message distribution,  $T_O$ ,  $\delta$ ,  $\sum_{k=1}^n P_{kO}$ ,  $\sum_{k=1}^s P_{0m_k}$  are all fixed in Equation (3). The variables that determine the actual lifetime are

$\sum_{k=1}^n P_{kM}$  and  $z$ . The smaller  $\sum_{k=1}^n P_{kM}^{\ddagger}$  is, the better the performance lower bound is. And the smaller  $z$  is, the better the performance lower bound is. However, a small  $z$  will lead to a large  $\sum_{k=1}^n P_{kM}$ . This explains the trade-off between minimal power path and max-min path.

Theorem 2 can be used in applications that have a regular message distribution without the restriction that all the messages are the same in two different slots. For these applications, the ratio between  $\delta$  and  $\sum_{k=1}^s P_{0m_k}$  must be changed to  $1/\sum_{k=1}^r P_{0m_k}$ , where  $P_{0m_k}$  is the minimal power consumption for the message generated in a unit of time.

### Theorem 3

*The optimal lifetime of the network is at most  $(t_{SPT} \cdot \sum P_h)/(\sum P_h - \sum P_h^{SPT})$  where  $t_{SPT}$  and  $P_h^{SPT}$  are the lifetime of the network and the remaining power of host  $h$  by using the least power-consumption routing strategy.  $P_h$  is the initial power of host  $h$ .*

**Proof:**

$$\begin{aligned} t_{OPT} &\leq \frac{\sum P_h}{\sum P_m^{SPT}} = \sum P_h / \left( \frac{\sum P_h - \sum P_h^{SPT}}{t_{SPT}} \right) \\ &= \frac{t_{SPT} \cdot \sum P_h}{\sum P_h - \sum P_h^{SPT}} \quad \square \end{aligned}$$

## 5. Hierarchical Routing Using Zone-based max-min $zP_{min}$

Although it has very nice theoretical and empirical properties, the max-min  $zP_{min}$  algorithm is hard to implement on large-scale networks. The main obstacle is that max-min  $zP_{min}$  requires accurate power level information for all the nodes in the network. It is difficult to collect this information from all the nodes in the network. One way to do it is by broadcast, but this would generate a huge power consumption that defeats our original goals. Furthermore, it is not clear how often such a broadcast would be necessary to keep the network data current. In this section we propose a hierarchical approach to power-aware routing that does not use as much information, does not

know the message sequence, and relies in a feasible way on max-min  $zP_{min}$ .

We propose to organize the network structurally in geographical zones, and hierarchically to control routing across the zones. The idea is to group together all the nodes that are in geographic proximity as a zone, treat the zone as an entity in the network, and allow each zone to decide how to route a message across<sup>§</sup>. The hosts in a zone autonomously direct local routing and participate in estimating the zone power level. Each message is routed across the zones using information about the zone power estimates. In our vision, a global controller for message routing manages the zones. This may be the node with the highest power, although other schemes such as round-robin may also be employed.

If the network can be divided into a relatively small number of zones, the scale for the global routing algorithm is reduced. The global information required to send each message across is summarized by the power-level estimate of each zone. We believe that in sensor networks this value will not need frequent updates because observable changes will occur only after long periods of time.

The rest of this section discusses (i) how the hosts in a zone collaborate to estimate the power of the zone; (ii) how a message is routed within a zone; and (iii) how a message is routed across zones. The max-min  $zP_{min}$  algorithm will be used in (i) and (ii), which can be implemented in a distributed way by slightly modifying our definition of the max-min  $zP_{min}$  path. The max-min algorithm used in (iii) is basically the Bellman-Ford algorithm, which can also be implemented as a distributed algorithm.

### 5.1. Zone Power Estimation

The power estimate for each zone is controlled by a node in the zone. This estimation measures the number of messages that can flow through the zone. Since the messages come from one neighboring zone and get directed to a different neighboring zone, we propose a method in which the power estimation is done relative to the direction of message transmission.

The protocol employed by the controller node consists of polling each node for its power level followed by running the max-min  $zP_{min}$  algorithm. The returned value is then broadcast to all the zones in the system. The frequency of this procedure is inversely

<sup>‡</sup> This is the remaining power of the network at the limit of the network.

<sup>§</sup> This geographical partitioning can be implemented easily using GPS information from each host.

proportional to the estimated power level. When the power level is high, the power estimation update can be done infrequently because messages routed through the zone in this period will not change the overall power distribution in the entire network much. When the power level is low, message transmission through the zone is likely to change the power distribution significantly.

Without loss of generality, we assume that zones are square so that they have four neighbors pointed to the North, South, East, and West<sup>¶</sup>. We assume further that it is possible to communicate between the nodes that are close to the border between two zones, so that in effect the border nodes are a part of both zones. In other words, neighboring zones that can communicate with each other have an area of overlap (see Figure 7a).

The power estimate of a zone can be approximated as follows. We can use the *max-min*  $zP_{min}$  algorithm to evaluate the power level, find the *max-min*  $zP_{min}$  path, simulate sending  $\Delta$  messages through the path, and repeat until the network is saturated.  $\Delta$  is chosen to be proportionate to the power level of the zone.

More precisely, consider Figure 7(a). To estimate the power of zone *B* with respect to sending messages in the direction from *A* to *C*, let the left part of the overlap between *A* and *B* be the source area and the right part of the overlap between *B* and *C* be the sink area. The power of zone *B* in the direction from *A* to *C* is the maximal number of messages that can flow from the source nodes to the sink nodes before a node in *B* gets saturated. This can be computed with the *max-min*  $zP_{min}$  algorithm (see Algorithm 3). We start with the power graph of zone *B* and augment it.

<sup>¶</sup> This method can easily be generalized to zones with finite number of neighboring zones.

We create an imaginary source node *S* and connect it to all the source nodes. We create an imaginary sink node *T* and connect all the sink nodes to it. Let the weights of the newly added edges be 0. The *max-min*  $zP_{min}$  algorithm run on this graph determines the power estimate for zone *B* in the direction of *A* to *C*.

**Algorithm 3** An approximation algorithm for zone power evaluation.

- 1: choose  $\Delta$  for the message granularity.  $P = 0$
- 2: **while** no node is depleted of power **do**
- 3: Find the *max-min*  $zP_{min}$  path for  $\Delta$  messages
- 4: send the  $\Delta$  messages through the zone
- 5:  $P = P + \Delta$
- 6: **return**  $P$

### 5.2. Global Path Selection

Given power-levels for each possible direction of message transmission, it is possible to construct a small zone-graph that models the global message routing problem. Figure 8 shows an example of a zone graph. A zone with *k* neighbors is represented by *k* + 1 vertices in this graph<sup>||</sup>. One vertex labels the zone; *k* vertices correspond to each message direction through the zone. The zone label vertex is connected to all the message direction vertices by edges in both direction. In addition, the message direction vertices are connected to the neighboring zone vertices if the current zone can go to the next neighboring zone in that direction. Each zone vertex has a power level of  $\infty$ . Each zone-direction vertex is labeled by its estimated power level computed with the procedure

<sup>||</sup> For square zones  $k = 4 + 1$  as shown in Figure 8.

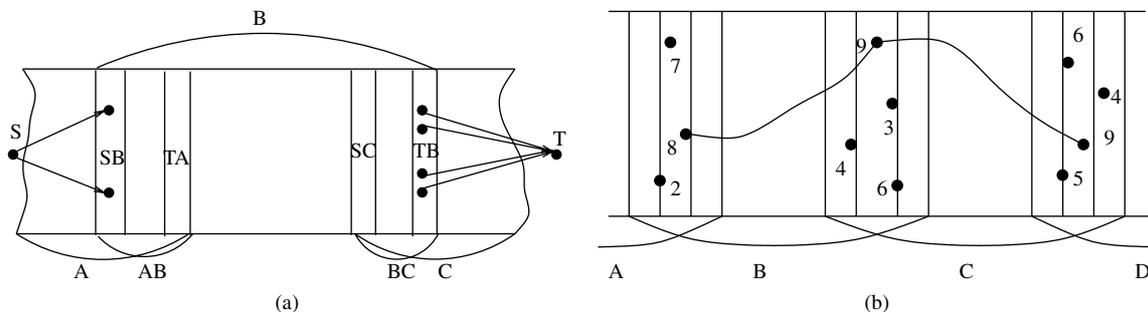


Fig. 7. Three zones, *A*, *B*, and *C*. *SB*, *SC* are the source areas of *B* and *C*, and *TA*, *TB* are the sink areas of *A* and *B*. *AB* and *BC* are overlap border areas. (b) shows how to connect the local path in zone *B* with the local path in zone *C*. The number next to each node is the number of paths passing through that node in the power evaluation procedure. The vertical stripes are the source and sink areas of the zones.

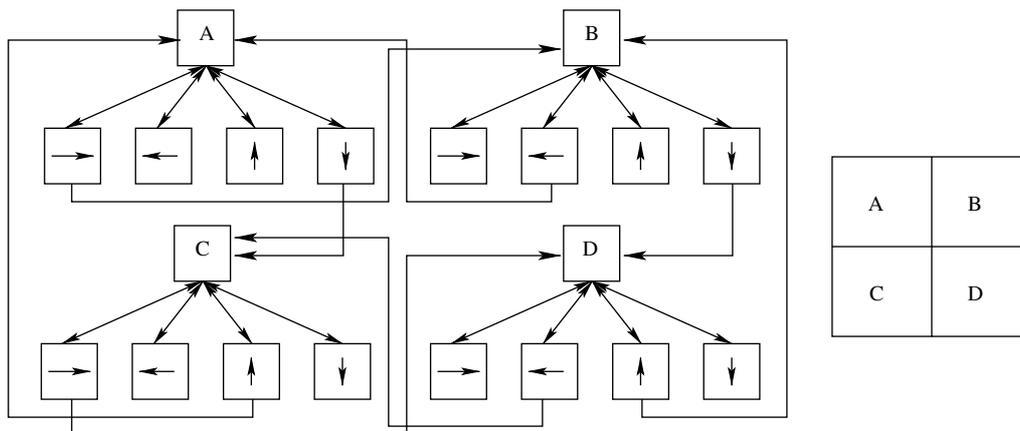


Fig. 8. Four zones are in a square network field. The power of a zone is evaluated in four directions, left, right, up, and down. A zone is represented as a zone vertex with four direction vertices. The power labels are omitted from this figure.

in Section 5.1. Unlike in the model we proposed in Section 3.1, the edges in this zone graph do not have weights. Thus, the global route for sending a message can be found as the *max-min* path in the zone graph that starts in the originator's zone vertex and ends in the destination zone vertex for the message. We would like to bias toward a path selection that uses the zones with higher power level. We can modify the Bellman-Ford algorithm (Algorithm 4) to accomplish this.

#### Algorithm 4 Maximal minimum power level path

- 1: Given graph  $G(V, E)$ , annotated with power level  $p(v)$  for each  $v \in V$
- 2: Find the path from  $s$  to  $t$ ,  
 $s = v_0, v_1, \dots, v_{k-1}, v_k = t$  such that  
 $\min_{i=1}^{k-1} p(v_i)$  is maximal
- 3: **for** each vertex  $v \in V[G]$  **do**
- 4:     **if** edge  $(s, v) \in E[G]$  **then**
- 5:          $d[v] \leftarrow \infty, \pi[v] \leftarrow s$
- 6:     **else**
- 7:          $d[v] \leftarrow 0, \pi[v] \leftarrow NIL$
- 8:  $d[s] \leftarrow \infty$
- 9: **for**  $i \leftarrow 1$  **to**  $|V[G]| - 1$  **do**
- 10:     **for** each edge  $(u, v) \in E[G]$  and  $u \neq s$  **do**
- 11:         **if**  $d[v] < \min(d[u], p[u])$  **then**
- 12:              $d[v] \leftarrow \min(d[u], p[u])$
- 13:              $\pi[v] \leftarrow u$
- 14: **return**  $\pi[t]$

#### 5.3. Local Path Selection

Given a global route across zones, our goal is to find actual routes for messages within a zone. The

*max-min*  $zP_{min}$  algorithm is used directly to route a message within a zone.

If there are multiple entry points into the zone, and multiple exit points to the next zone, it is possible that two paths through adjacent zones do not share any nodes. These paths have to be connected.

The following algorithm is used to ensure that the paths between adjacent zones are connected (see Figure 7b). For each node in the overlap region, we compute how many paths can be routed locally through that node when the zone power is evaluated. In order to optimize the message flow between zones, we find paths that go through the nodes that can sustain the maximal number of messages. Thus, to route a message through zone  $B$  in the direction from  $A$  to  $C$  we select the node with maximum message weight in the overlap between  $A$  and  $B$ , then we select the node with maximum message weight in the overlap between  $B$  and  $C$ , and compute the *max-min*  $zP_{min}$  paths between these two nodes.

#### 5.4. Performance Evaluation for Zone-based Routing

The zone-based routing algorithm does not require as much information as would be required by the *max-min*  $zP_{min}$  algorithm over the entire network. By giving up this information, we can expect the zone-based algorithm to perform worse than the *max-min*  $zP_{min}$  algorithm. We designed large experiments to measure how the zone-based algorithm does relative to the *max-min*  $zP_{min}$  algorithm. (In the following experiments, we only consider the power consumption used for the application messages instead of the control messages. Thus, we can compare how

close the performance of our zone-based algorithm is to that of the *max-min*  $zP_{min}$  algorithm without the influence of the control messages.)

We disperse 1 000 nodes randomly in a regular network space (see Figure 9). The zone partition is described in the figure. Each zone has an average of 40 nodes. Each node sends one message to a gateway node in each round (A round is the time for all the nodes to finish sending messages to the gateway). The zone power-evaluation protocol is executed after each round. By running the *max-min*  $zP_{min}$  algorithm, we ran the algorithm for about 41 000 messages before one of the hosts got saturated. By running the zone-based routing algorithm, we got about 39 000 messages before the first message could not be sent through. The performance ratio between the two algorithms in terms of the lifetime of the network is 94.5%. Without the zone structure, the number of control messages on the power of each node in every information update is 1000, and they need to be broadcast to 1000 nodes. In the zone-based algorithm, the number of control messages is just the number of the zones, 48 in this case, and they are broadcast to 24 zones after the zone power evaluation. In addition, the zone-based routing dramatically reduces the running time to find a route in our simulation. In another experiment, we disperse 1240 sensors

to a square field with size  $6.2 * 6.2$ . The sensors are distributed randomly in the field. Each sensor has an initial power of 400. The power consumption formula is  $e_{ij} = 10 * d_{ij}^3$ . The network field is divided by  $5 * 5$  squares each of which corresponds to four zones in four directions (left, right, up, and down). The zone-based algorithm achieved 96% of the lifetime of the *max-min*  $zP_{min}$  algorithm.

### 6. Distributed Power-Aware Routing with *max-min* $zP_{min}$

The algorithms discussed in the previous sections do not work for applications in which it is impossible to control in a centralized way the message flow in the ad hoc network. Applications in which nodes move frequently and unpredictably fall in this category. In this section we investigate a class of routing algorithms for which computation is distributed and information localized.

We introduce three new algorithms: a distributed minimal power algorithm, a distributed *max-min* power algorithm, and the distributed *max-min*  $zP_{min}$  power-aware algorithm. The first two algorithms are used to define the third, although they are very interesting and useful in their own right for applications

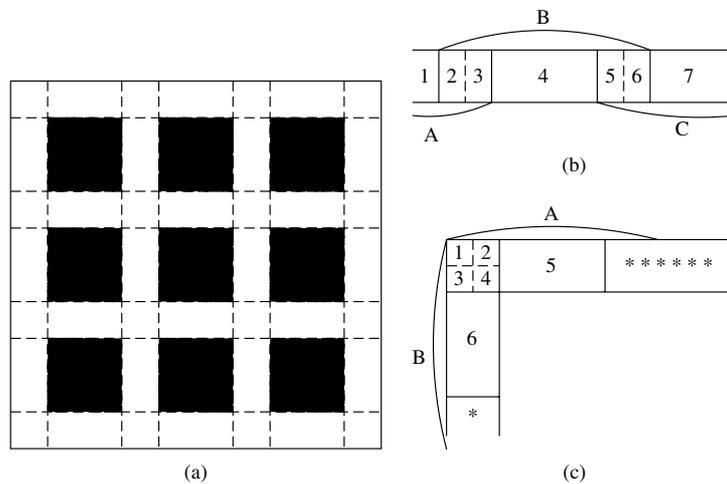


Fig. 9. The scenario used for the zone-based experiment. The network space is a  $10 * 10$  square with nine buildings blocking the network. Each building is of size  $2 * 2$ , and regularly placed at distance 1 from the others. The sensors are distributed randomly in the space near the buildings. Each sensor has an initial power of 4000. The power consumption formula is  $e_{ij} = 10 * d_{ij}^3$ . We partition the network space into 24 zones, each of which is of size  $1 * 4$  or  $4 * 1$ , depending on its layout. For each zone, there is another corresponding zone with the same nodes but with opposite directions. For example, in (b), areas 2, 3, 4, 5, 6 constitute a zone, with 2 and 6 its source and sink areas; and 6, 5, 4, 3, 2 constitute another zone with 6 and 2 its source and sink areas. We have a total of 48 zones. (b) and (c) show the layout of the neighboring zones. In (b), 3 is the sink area of the zone A, and 5 is the source area of zone C. The border area of A and B is 2, 3; and the border area of B and C is 5, 6. (c) shows two perpendicular zones. The source area of B is 1, 2. The border area of A and B is 1, 2, 3, 4.

in which the optimization criteria are the minimum power and the maximum residual power, respectively.

### 6.1. A Distributed Minimal Power Algorithm

We can develop a distributed version of Dijkstra's algorithm that is guaranteed to be a minimal-power path, by giving messages variable propagation delays. The idea is to have messages traveling along short paths move faster than messages traveling along long paths. Thus, messages traveling along shorter paths will arrive faster than messages traveling along longer paths—that is, the algorithm will select the shortest paths. In this case, the Dijkstra distance corresponds to power consumption.

We can implement this idea by augmenting each message with a record of how far it traveled from the base to the current node. This information is represented by a variable attached to the message that measures the cost (distance representing power consumption). Algorithm 5 is the resulting minimal power path algorithm, which represents a distributed version of Dijkstra's algorithm.

We continue this section by arguing that Algorithm 5 produces the minimal power-consumption path for each node. Furthermore, the running time of the algorithm is proportional to the longest shortest distance from the base node to any node.

We first examine a special case—when messages are time-sorted in the following sense. Suppose two messages carrying 'distance' values  $v_1$  and  $v_2$  arrive at the same node at time  $t_1$  and  $t_2$ . If for any two messages with  $v_1 < v_2$ , we have  $t_1 < t_2$ , the messages are *time-sorted*. Let  $n$  be the number of nodes in the network. In order to keep our proof simple, we assume that message transmission is instantaneous—this restriction can be relaxed.

**Theorem 4** *If the messages are time-sorted, then Algorithm 5 requires  $O(n)$  broadcasting messages ( $O(1)$  for each node).*

**Proof:** Let the message value of a message be the distance from the base station to the current node. Since the messages are time-sorted, the earliest message must carry the shortest distance from the base station to the current node. By line 9 of the algorithm, this message will be broadcast only once after the  $t_B$  waiting period has been completed.

**Algorithm 5** *Minimal Power Path.* The input consists of a network system in which each node can

determine its location and its power level. The output is the minimal-power routing table at each node (with respect to communicating to the base.) The algorithm uses the following parameters:  $\eta$  is the unit power for transforming the power level into waiting time;  $P_A$  is the total power consumption of the optimal path found so far from  $A$  to the base node;  $e(A, B)$  is the power consumption of sending one message from  $A$  to  $B$  directly;  $t_B$  is the earliest time for  $B$  to broadcast the routing message;  $N_B$  is the route of node  $B$ .

- 1: **Initialization;** may not be necessary
- 2: Handshaking among neighbors; each node broadcasts its id, its position, and its current power level
- 3:  $P_B = \infty, t_B = \infty$
- 4: **if I am base station then**
- 5:   initiate the message broadcasting
- 6: **else if I am not base, say my id is  $B$  then**
- 7:   Receive message  $(A, P_A)$ ; get the sender id  $A$  and  $P_A$  from the message
- 8:   Compute  $P_B = \min(P_A + e(A, B), P_B)$  and  $t_B = \min(t_B, \eta P_B)$   
    **if  $P_B = P_A + e(A, B)$  then**  
     $N_B = A$
- 9:   Wait till the current time is  $t_B$ , broadcast the message  $(B, P_B)$  to its neighbors, and stop

In Algorithm 5, the messages are not time-sorted. However, the messages become time-sorted if we consider the broadcast time of a node as the message arrival time (because of the delays enforced by the algorithm) and by Theorem 4, Algorithm 5 gives the shortest path within  $O(n)$  broadcasts.

Note that the performance of our algorithm depends on the granularity at which we can measure power. Let the smallest measurement unit of the power consumption or the tolerable measurement unit be  $s$ . The parameter  $\eta$ , which can be chosen as the smallest time unit a node can distinguish, is the waiting time that corresponds to the distance  $s$ . The running time of Algorithm 5 is proportional to  $1/s$  and to the size of the largest minimal power path. A large value for  $s$  results in a fast running time, but at the expense of precision. Say, two messages that travel along paths with power consumption of  $P$  and  $P + s_1$  (where  $s_1 < s$ ) arrive at the same node in an interval less than  $\eta$ . The node may not distinguish them because the time difference is too small. Therefore, the running time is dependent on the precision of the required power consumption measurement. A better running

time can be obtained by allowing a low measurement precision, that is, a large unit power consumption  $\eta$ .

Algorithm 6 summarizes our ideas for improving the performance.

**Algorithm 6** *The second minimal-power path algorithm.* The input is a network in which each node can determine its location and its power level. The output is a routing table for each node. The parameters are  $P_A$ , the total power consumption of the optimal path found so far from  $A$  to the base node;  $e(A, B)$ , the power consumption of sending a message from  $A$  to  $B$  directly; and  $\delta$ , the unit time corresponding to each power slot ( $P/m$ ), used to transform the power level into waiting time;  $N_B$ : the route of node  $B$ .

- 1: **Initialization**; may not be necessary
- 2: Handshaking among neighbors: each node broadcasts its id, its position, and its current power level
- 3: The base initiates the message broadcasting
- 4: **if** I am not the base **then**
- 5:   Let my id be  $B$
- 6:    $P_B = \infty$ . Initial time is 0.
- 7:   Receive message  $(A, P_A)$ ; get the sender id  $A$  and the power  $P_A$  from the message
- 8:   Compute the new power  $P_B = \min(P_B, P_A + e(A, B))$ , and find the proper slot  
 $i = \lfloor m \cdot P_B / P \rfloor$
- if**  $P_B = P_A + e(A, B)$  **then**  
 $N_B = A$
- 9:   Set waiting timer to  $i\delta$  (i.e. the time point when a broadcast happens)
- 10:   **if** the current time is no less than the waiting time point **then**
- 11:     broadcast the message  $(B, P_B)$  to its neighbors, and clear the timer.; We do that because there may be several paths being broadcast to the node. But their time must be between  $i\delta$  and  $(i+1)\delta$
- 12:   **if** the current time is  $(i+1)\delta$  **then**
- 13:     stop

We assume the maximal minimal power consumption from the base station to any node in the network  $P$ . Let's divide  $[0, P)$  into  $m$  slots,  $[0, P/m)$ ,  $[P/m, 2P/m)$ ,  $\dots$ ,  $[iP/m, (i+1)P/m)$ ,  $\dots$ ,  $[(m-1)P/m, P)$ . When a node receives a message with value  $v$ , it first finds the  $i^{\text{th}}$  slot such that  $iP/m \leq v < (i+1)P/m$ , waits till time  $i\delta$ , and then broadcasts the message to its neighbors. The running time of the algorithm ( $m\delta$ ) is proportional to  $m$  and the

parameter  $\delta$ , which is the time interval corresponding to  $P/m$ .

We can choose  $\delta$  to be large enough that any message traveling from the base station to any node in the network along a minimal power path will have a total message processing time  $\varepsilon < \delta$  (i.e. the sum of the message-processing time at each node on the minimal power path is less than  $\delta$ ).

**Theorem 5** *For Algorithm 6, the number of messages broadcast by each node is no greater than the maximal number of paths from the base to a node with the power consumption in the same slot as that of the minimal power path (i.e.  $[iP/m, (i+1)P/m)$  in which the minimal power consumption lies).*

**Proof:** Consider a message arriving at node  $A$  and scheduled to be broadcast in the slot  $[i\delta, (i+1)\delta)$ .

The message traveling along the minimal power path arrives at  $A$  at some time point before  $i\delta + \varepsilon$  since we assume the total message handling time (including message buffering, queuing, and propagation) is less than  $\varepsilon$ .

A message traveling along a path with power no less than  $(i+1) \cdot P/m$  will not be scheduled to be broadcast because the node stops broadcasting at time  $(i+1)\delta$ .

There is no path with power consumption less than  $i \cdot P/m$  to that node, so no message can be broadcast before  $i\delta$  by that node.

Thus, only the messages traveling along the paths with power in the range of  $[P_{\min}, (i+1)\delta)$  can be scheduled to be broadcast.

**Theorem 6** *Algorithm 6 gives the minimal power consumption route for each node.*

**Proof:** The message traveling along the minimal power path arrives at  $A$  at some time point before  $i\delta + \varepsilon < (i+1)\delta$  since we assume the total message handling time (including message buffering, queuing, and propagation) is less than  $\varepsilon$ . There is no path with power consumption less than  $i \cdot P/m$  to that node, so no message can be broadcast before  $i\delta$  by that node.

Thus, the message traveling along the minimal power path will be broadcast at each node. Then each node can look at the power consumption value carried by the message and set the node that broadcast the message as its route.  $\square$

## 6.2. A Distributed max–min Algorithm

The minimal power path algorithm does not consider the residual powers of nodes when computing the route. Although a packet is routed along the minimal power path, some nodes on that path may be saturated very quickly. An alternative is to use the nodes with high power and avoid the nodes that are almost saturated, which leads to the max–min path for packet routing.

The max–min path is defined as the route from a node to the base on which the minimal residual power of the nodes is maximized among all the routes. The minimal residual power of a path  $p(c, d)$  is  $c = a_1, a_2, \dots, a_k = d$ , as  $m_{p(c,d)} = \min_{i=1}^{n-1} (P(a_i) - e(a_i, a_{i+1})) / (P(a_i))$ , and the max–min value  $F_{(c,d)} = \max_{all\ p(c,d)} m_{p(c,d)}$ . If there may be multiple routes with the same max–min residual power, we can resolve ties arbitrarily.

Max–min paths can be found by using a modified version of the distributed Bellman–Ford algorithm. Upon computing a new max–min value, each node broadcasts it. The neighbors compute their max–min value according to the new incoming value, and broadcast the result only if the value is changed. The number of message broadcasts may be  $O(n^3)$  as in the case of the distributed Bellman–Ford algorithm.

To reduce the message broadcasts, we employ the same method as in Section 6.1 and add a variable waiting time on each node, which controls when the node broadcasts. Algorithm 7 summarizes the resulting protocol. We assume all the nodes are synchronized well, so they can decide locally the global time. Thus, a global clock is not needed to make this protocol work.

### Algorithm 7 Distributed Max–min Approximation.

The input is a network in which each node can determine its location and its power level. The output is a routing table at each node. The parameters are:  $P(A)$ , the current power level of node  $A$ ;  $e(A, B)$ , the power consumption of sending one message from  $A$  to  $B$  directly; and  $\delta$ , the unit time corresponding to each power slot ( $P/m$ ) used to transform the power level into waiting time.

- 1: **Initialization**; may not be necessary
- 2: Handshaking among neighbors: each node broadcasts its id, its position, and its current power level
- 3: For each node  $B$ , let  $F_B = 0$ ,  $B$  does the following for  $i = m - 1, m - 2, \dots, 1, 0$ .

- 4: The base node initiates the search and broadcasts the maximal max–min value
- 5: **if** Node  $B$  receive a message  $(A, P(A), F_A)$  from its neighbor  $A$  **then**
- 6: According to the power level of  $A$  and the distance between  $A$  and  $B$ , compute  $F_B = \max \left( F_B, \min \left( F_A, \frac{P(A) - e(A, B)}{P(A)} \right) \right)$
- 7: **if**  $F_B = \min \left( F_A, \frac{P(A) - e(A, B)}{P(A)} \right)$  **then**
- 8:      $N_B = A$
- 9: **if**  $(i + 1)F_{max}/m > F_B \geq iF_{max}/m$  **then**
- 10:     the max–min value of  $B$  is found
- 11:      $B$  broadcasts the message  $(B, P(B), F(B))$ , the next node in the routing table is  $A$ , stop
- 12: After time  $\delta$ ,  $i = i - 1$ ; go to 5

The max–min approximation, Algorithm 7 considers the maximal residual power fraction of all nodes in the network  $F_{max}$  split into  $m$  slots ( $[0, F_{max}/m), [F_{max}/m, 2F_{max}/m), \dots, [iF_{max}/m, (i + 1)F_{max}/m), \dots, [(m - 1)F_{max}/m, F_{max})$ ). The  $m$  slots are mapped to consecutive  $\Delta$  long time slots ( $s_1, s_2, \dots, s_m$ ). In  $s_i$  the algorithm will find all the nodes whose max–min values are in slot  $[(i - 1)F_{max}/m, iF_{max}/m]$ . The nodes found in the earlier slots have higher max–min values in the later slots.

We assume that the base has the maximal max–min value in the beginning of the algorithm. Thus, the base initiates the algorithm in the first slot  $s_1$ . Upon receiving the max–min values from the neighbors, nodes update their max–min value. Nodes wait until the time slot corresponding to the current max–min value, and broadcast the value to its neighbors. If the node receives a new incoming value in some slot, say  $s_i$ , and finds that its max–min value should also be broadcast in this time slot, the broadcast is immediate. Thus, the nodes with max–min values in  $[(i - 1)F_{max}/m, iF_{max}/m]$  will be found as the messages go around the whole network.

If all the nodes have synchronized clocks, this algorithm performs  $O(1)$  message broadcasts for each node. Otherwise, the base must initiate a synchronized broadcast to all the nodes to start a new slot and the number of broadcasts per node becomes  $O(m)$ .

Since each node broadcasts at most  $m$  messages, the running time of the algorithm is  $m\delta$  where  $\delta$  is the time for each round, which is at most  $n$  times the per message handling time. Furthermore, we can prove the following result using induction.

**Theorem 7** For each node, the algorithm gives a route with the minimal residual power fraction  $F$ , such

that  $F$  and  $F^m$  are in the same slot where  $F^m$  is the max–min power fraction of the route from the base to that node. Then we have  $|F - F^m| \leq F_{max}/m$ .

**Proof:** We use induction. In the first round, the maximal max–min value is broadcast by the base node. Each node that has the max–min value in the slot will broadcast the message.

For any node  $B$  with max–min value  $F_B^m$  in slot  $i$ , it is impossible for  $B$  to broadcast its value in slots before  $i$ . That is,  $F_B$  must be no greater than  $F_B^m$ , the actual max–min value of node  $B$ . This can be derived by examining the computation of  $F_B$ .

Suppose each node that finishes broadcast has  $F$  and  $F^m$  in the same slot. For any node  $B$  whose max–min value is in slot  $i$ , let  $A$  be the upstream node on the max–min path from the base to  $B$ . If  $B$  broadcasts its max–min value before  $A$ , then  $B$  can determine  $A$ 's slot. Otherwise,  $A$  must broadcast its max–min value before  $B$  and  $B$  will hear the max–min value of  $A$ . Thus, from the algorithm, we have (see Algorithm 7)  $\min(F_A^m, (P(A) - e(A, B))/(P(A))) = F_B^m \geq F_B \geq \min(F_A, (P(A) - e(A, B))/(P(A)))$ . From Step (3), we know  $\min(F_A^m, (P(A) - e(A, B))/(P(A)))$  and  $\min(F_A, (P(A) - e(A, B))/(P(A)))$  are in the same slot, so we know  $F_B$  and  $F_B^m$  are in the same slot.  $\square$

We can improve Algorithm 7 by using binary search. The running time can be reduced to  $\delta \log m$ , but the number of total messages sent is  $n \log m$ . The key idea is to split the range  $[0, F_{max}]$  in two,  $[0, F_{max}/2]$  and  $[F_{max}/2, F_{max}]$ . In the first epoch, the algorithm tries to find all the nodes whose max–min values are in the higher half. In the second epoch, we split each range into two halves to get four ranges. The algorithm finds in parallel all the nodes whose max–min values are in the higher half of each range, and so on.

### 6.3. Distributed max–min $zP_{min}$

We now derive the distributed version of the centralized online max–min  $zP_{min}$  algorithm. Like in the centralized case, our motivation is to define a routing algorithm that optimizes the overall lifetime of the network by avoiding nodes of low power, while not using too much total power. There is a trade-off between minimizing the total power consumption and maximizing the minimal residual power of the network. We propose to enhance a max–min path by limiting its total power consumption.

Recall that the network is described as a graph in which each vertex corresponds to a node in the network, and only two nodes within the transmission ranges of each other have an edge connecting them in the graph. The power level of a node  $a$  is denoted as  $P(a)$ , and the power consumption to send a message unit to one of its neighbors  $b$  is denoted as  $e(a, b)$ . Let  $s(a)$  be the power consumption for sending a unit message from  $a$  to the base station along the least power consumption path. Let  $r(a)$  be the minimum residual power fraction of the nodes on  $a$ 's  $mmz$  path. Let  $P_a$  be the power consumption along the  $mmz$  path.

An  $mmz$  path has the following properties:

1. it consists of two parts: the edge connecting  $a$  to one of its neighbors and the  $mmz$  path of that neighbor;
2. its total power consumption is less than or equal to  $z \cdot s(a)$ ; and
3. among all those paths defined by (1) and (2), the max–min value of the  $mmz$  path is maximized.

More precisely,  $p(a)$ , the  $mmz$  path of node  $a$ , is (i) a simple path from  $a$  to the base station; (ii)  $f_a < z \cdot s(a)$ ; and (iii)  $p(a) = (a, b) \cup p(b)$ , where  $b$  is  $a$ 's neighbor such that for any other neighbor  $c$   $r(a) = \min(r(b), (P(a) - e(a, b))/(P(a))) \geq \min(r(c), (P(a) - e(a, c))/(P(a)))$ .

**Theorem 8** *There is one node  $b_j$  such as  $e(a, b_j) + P_{b_j} \leq z \cdot s(a)$ .*

**Proof:** Use induction. The case for the base is obvious. Let  $b_j$  be the node on the shortest path from  $a$  to the base.  $f_{b_j} \leq z \cdot s(b_j)$  and  $e(a, b_j) + s(b_j) = s(a)$ . So  $e(a, b_j) + f_{b_j} \leq e(a, b_j) + z \cdot s(b_j) \leq z \cdot (e(a, b_j) + s(b_j)) = z \cdot s(a)$ .  $\square$

Note that  $s(a)$  can be computed easily by using  $s(a) = \min \{s(b) + e(a, b)\}$  where  $b$  is  $a$ 's neighbor.

The definition of the  $mmz$  path actually gives a constructive method for computing incrementally the  $mmz$  path by keeping track of  $s(node)$ ,  $r(node)$ ,  $p(node)$  of each node  $n$ , because the computation only depends on these values at  $v$ 's neighbors. Let  $n(node)$  be the next node on the path  $p(node)$ . The resulting algorithm is shown as Algorithm 8. In the algorithm, the base station initiates the route exploration by broadcasting its route information ( $s(base)$ ,  $r(base)$ , and  $n(base)$ ) to

its neighbors). When a node's route information changes, it broadcasts its updated information. This broadcast triggers its neighbor nodes to check if their route information changes. Every time the route information of a node changes the information is broadcast until the system achieves equilibrium.

**Algorithm 8** *Distributed max-min  $zP_{min}$* . The parameters are  $P_{min}^B$ , the minimal power consumption for node  $B$  to send a message to the base;  $P_B$ , the power consumption of the path discovered so far from the node to the base;  $P(B)$ , node  $B$ 's current power level;  $F_B$ , the maximal min residual power level of the found route to base from node  $B$ ; and  $N_B$ : the next node on  $B$ 's found route.  $\delta$  is an algorithm-dependent parameter; different implementations may have difference choices.

- 1: Find the minimal power consumption path for each node
- 2: The base node 0 initiates the route discovery
- 3:  $P_0 = 0$ ;  $F_0 = \infty$ ;  $N_0 = 0$
- 4: Node 0 sends route discovery request to its neighbors
- 5: Each node  $B$  receives message from its neighbors  $A_1, A_2, \dots, A_k$
- 6: It waits for time  $\delta$ , then compute:  
 $P_B = \min(P_{A_1} + e(B, A_1), P_{A_2} + e(B, A_2), \dots, P_{A_k} + e(B, A_k))$ . Find all the neighboring nodes such that  $P_{A_i} + e(B, A_i) \leq zP_{min}^{A_i}$ . Among all those neighbors found, find the node with maximal  $\min(F_{A_k}, (P(B) - e(B, A_k))/P(B))$ . Let the node be  $N_B$  and the min value be  $F_B$
- 7: Broadcast the  $P_B$  and  $F_B$  to its neighbors  
 Repeat 3, 4 until the routing table gets to equilibrium

In our distributed version of the max-min  $zP_{min}$  algorithm, we expect  $O(n^3)$  messages broadcast totally in the worst case.

It is possible to improve the number of message broadcasts by using timing variables to suppress some of the messages. Two specific approaches are

- In the max-min part, let the message carry the total power consumption on the path and use the power consumption to decide if the max-min value should be accepted.
- In the minimal power path part, incorporate the max-min value in the waiting time.

### 6.4. Experiments in Simulation

We have implemented the distributed algorithms outlined in this section and studied the performance of the distributed max-min  $zP_{min}$  algorithm. Furthermore, we compared this algorithm against a greedy-style distributed algorithm.

Figure 10 shows the concept behind our greedy routing implementation. Periodically, nodes exchange power information with their neighbors. When there is a message at  $A$  for destination  $D$ ,  $A$  finds the node  $B$  with the highest power level in its transmission range centered at  $A$  with angle  $\theta$ , which is bisected by line  $AD$ , and sends the message to  $B$ .

Figure 11 shows the performance comparison of the distributed max-min  $zP_{min}$  algorithm and the distributed greedy algorithm. We conclude that max-min  $zP_{min}$  outperforms a simple greedy algorithm for

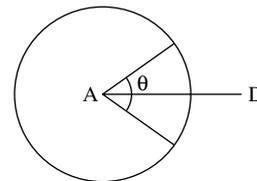


Fig. 10. The greedy routing method sends messages to the nearest neighbor within transmission range in a cone of directions captured by a parameter  $\theta$ .

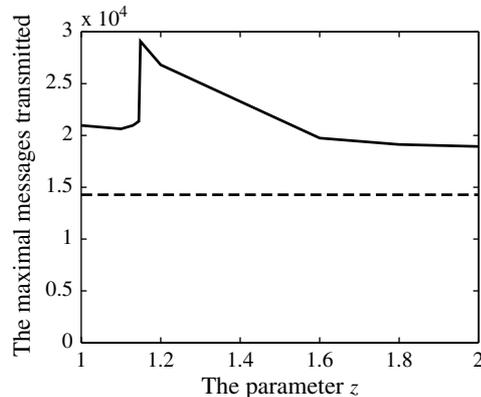


Fig. 11. The performance comparison of distributed max-min  $zP_{min}$  algorithm and greedy algorithm. The dashed line shows the performance of the greedy algorithm and the solid line shows the performance of the max-min  $zP_{min}$  algorithm. The network includes 100 nodes. The network space is  $100 * 100$ , the transmission range is 20, the power consumption formula is  $E = 2 * 10^{-6} * d^3$ . The greedy algorithm uses a  $\theta = \pi/3$ . The routing protocol is run after every 100 messages. The neighbor information update in the greedy algorithm is updated every 100 messages.

all values of  $z$ , and for some values of  $z$  the distributed  $max-min zP_{min}$  doubles the performance. More specifically, peak of the  $max-min zP_{min}$  algorithm is obtained when  $z = 1.2$ , and the number of messages sent is 29 078. When  $z = 2$ , the number message sent is the lowest at 18 935. The distributed greedy algorithm sent 14 278 messages in total. The performance improvement is 103% in the best case when  $z = 1.2$  and 32.61% in the worst case.

We are currently collecting empirical data on the trade-offs between the various parameters we introduced to describe our algorithms.

## 7. Conclusion

We have described several online algorithms for power-aware routing of messages in large networks dispersed over large geographical areas. In most applications that involve ad hoc networks made out of small handheld computers, mobile computers, robots, or smart sensors, battery level is a real issue in the duration of the network. Power management can be done at two complementary levels: (i) during communication and (ii) during idle time. We believe that optimizing the performance of communication algorithms for power consumption and for the lifetime of the network is a very important problem.

It is hard to analyze the performance of online algorithms that do not rely on knowledge about the message arrival and distribution. This assumption is very important as in most real applications the message patterns are not known ahead of time. In this paper we have shown that it is impossible to design an online algorithm that has a constant competitive ratio to the optimal off-line algorithm, and we computed a bound on the lifetime of a network whose messages are routed according to this algorithm. These results are very encouraging.

We developed an online algorithm called the  $max-min zP_{min}$  algorithm and showed that it had a good empirical competitive ratio to the optimal off-line algorithm that knows the message sequence. We also showed empirically that  $max-min zP_{min}$  achieves over 80% of the optimal (where the optimal router knows all the messages ahead of time) for most instances and over 90% of the optimal for many problem instances. Since this algorithm requires accurate power values for all the nodes in the system at all

times, we proposed a second algorithm that is hierarchical. Zone-based power-aware routing partitions the ad hoc network into a small number of zones. Each zone can evaluate its power level with a fast protocol. These power estimates are then used as weights on the zones. A global path for each message is determined across zones. Within each zone, a local path for the message is computed so as to not decrease the power level of the zone too much. Finally, we have developed a distributed version of the  $max-min zP_{min}$ , in which all the decisions use local information only, and showed that this algorithm outperforms significantly a distributed greedy-style algorithm.

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